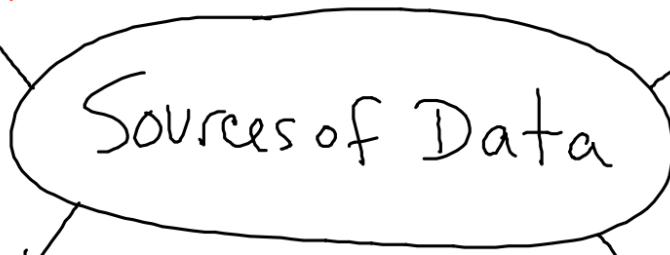


Sec 5.1

Observational
Studies

Sample Surveys
& Polls



Experimental
Studies

Simulations

Census

Gathers information on entire population

Sample

Part of a population

Bad Samples (Biased)

- Voluntary Response Samples
- Convenience Samples

Good / Scientific Samples

1) Simple Random Sample (SRS)

"Consists of n individuals from the population, chosen in a way that every set of n individuals has an equal chance to be part of the sample"

Not Ex 1 2 3 | 4 5 6 | 7 8 9 | 10 11 12

Choosing An SRS (Ex 5.10, P. 279)

1. Assign a numerical value to each individual
2. Use Random Digits Table or Calculator

↑
Same # of
digits!

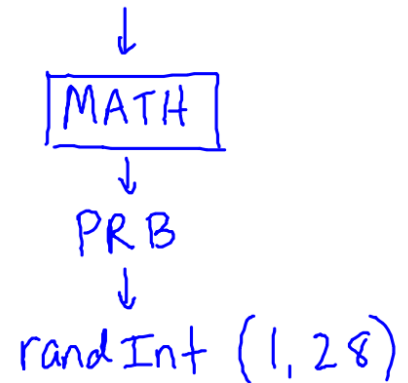
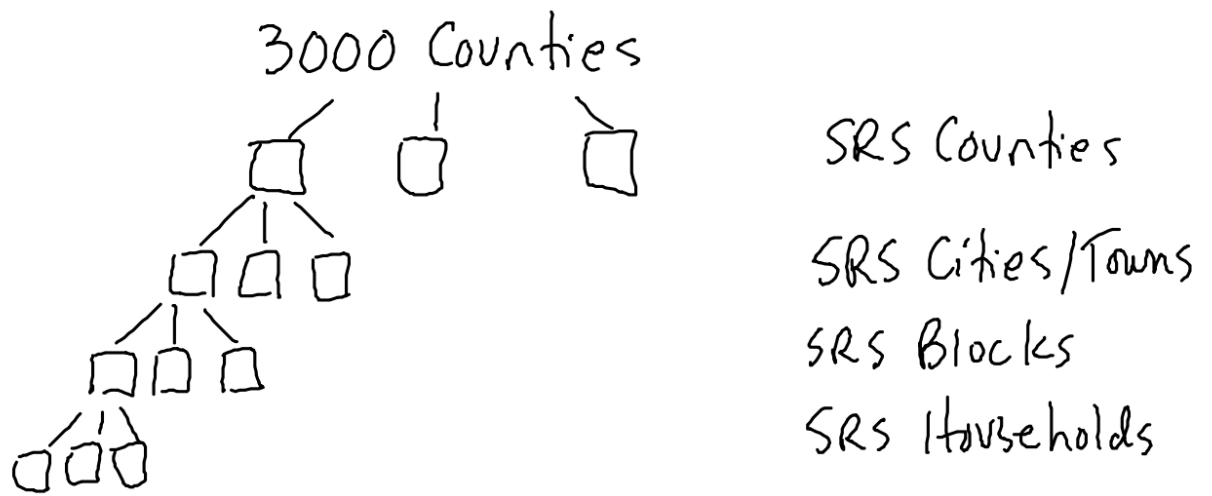


TABLE B Random digits

Line								
101	19223	95034	05756	28713	96409	12531	42544	82853
102	73676	47150	99400	01927	27754	42648	82425	36290
103	45467	71709	77558	00095	32863	29485	82226	90056
104	52711	38889	93074	60227	40011	85848	48767	52573
105	95592	94007	69971	91481	60779	53791	17297	59335
106	68417	35013	15529	72765	85089	57067	50211	47487
107	82739	57890	20807	47511	81676	55300	94383	14893
108	60940	72024	17868	24943	61790	90656	87964	18883
109	36009	19365	15412	39638	85453	46816	83485	41979
110	38448	48789	18338	24697	39364	42006	76688	08708
111	81486	69487	60513	09297	00412	71238	27649	39950
112	59636	88804	04634	71197	19352	73089	84898	45785
113	62568	70206	40325	03699	71080	22553	11486	11776
114	45149	32992	75730	66280	03819	56202	02938	70915
115	61041	77684	94322	24709	73698	14526	31893	32592
116	14459	26056	31424	80371	65103	62253	50490	61181
117	38167	98532	62183	70632	23417	26185	41448	75532
118	73190	32533	04470	29669	84407	90785	65956	86382
119	95857	07118	87664	92099	58806	66979	98624	84826
120	35476	55972	39421	65850	04266	35435	43742	11937
121	71487	09984	29077	14863	61683	47052	62224	51025
122	13873	81598	95052	90908	73592	75186	87136	95761
123	54580	81507	27102	56027	55892	33063	41842	81868
124	71235	09001	43367	49497	72719	96758	27611	91596
125	96746	12149	37823	71868	18442	35119	62103	39244
126	96927	19931	36809	74192	77567	88741	48409	41903
127	43909	99477	25330	64359	40085	16925	85117	36071
128	15689	14227	06565	14374	13352	49367	81982	87209
129	36759	58984	68288	22913	18638	54303	00795	08727
130	69051	64817	87174	09517	84534	06489	87201	97245
131	05007	16632	81194	14873	04197	85576	45195	96565
132	68732	55259	84292	08796	43165	93739	31685	97150
133	45740	41807	65561	33302	07051	93623	18132	09547
134	27816	78416	18329	21337	35213	37741	04312	68508
135	66925	55658	39100	78458	11206	19876	87151	31260
136	08421	44753	77377	28744	75592	08563	79140	92454
137	53645	66812	61421	47836	12609	15373	98481	14592
138	66831	68908	40772	21558	47781	33586	79177	06928
139	55588	99404	70708	41098	43563	56934	48394	51719
140	12975	13258	13048	45144	72321	81940	00360	02428
141	96767	35964	23822	96012	94591	65194	50842	53372
142	72829	50232	97892	63408	77919	44575	24870	04178
143	88565	42628	17797	49376	61762	16953	88604	12724
144	62964	88145	83083	69453	46109	59505	69680	00900
145	19687	12633	57857	95806	09931	02150	43163	58636
146	37609	59057	66967	83401	60705	02384	90597	93600
147	54973	86278	88737	74351	47500	84552	19909	67181
148	00694	05977	19664	65441	20903	62371	22725	53340
149	71546	05233	53946	68743	72460	27601	45403	88692
150	07311	88915	41267	16853	84569	79367	32337	03316

2) Stratified Random Samples

3) Multistage Random Samples



4) Systematic Random Samples

Choose every n^{th} person from a population - Exit Polling

Cautions / Issues

- Undercoverage
- Nonresponse
- Response Bias
- Wording Effect
- Sample Size

How Are Polls Conducted?

Public opinion polls would have less value in a democracy if the public -- the very people whose views the polls represent -- didn't have confidence in the results. This confidence does not come easily. The process of polling is often mysterious, particularly to those who don't see how the views of 1,000 people can represent those of hundreds of millions. Many Americans contact Gallup each year:

1. to ask how Gallup's results can differ so much from their own personal impressions of what people think;
2. to learn how Gallup selects people for inclusion in its polls; and
3. to find out why they have never been interviewed.

The public's questions indicate a sincere desire to find out more about how polling is actually conducted, which this FAQ section will address.

The Sampling Issue

Probability sampling is the fundamental basis for all survey research. The basic principle: If selected correctly, a randomly selected small sample of a population of people *can* represent the attitudes, opinions, or projected behavior of all of the people from which the sample is obtained.

The fundamental goal of a survey is to come up with the same results that would have been obtained had every member of a population been interviewed. For national Gallup polls, in other words, the objective is to represent the opinions of a sample of people who hold the same opinions that would have been obtained if it were possible to interview all adult Americans in the country. There are difficulties involved at every step of the process of attempting to reach this goal, but this overall objective stands as the central organizing principle for Gallup's methodological procedures.

The key to reaching this objective is a fundamental principle called *equal probability of selection*, which states that if every member of a population has an equal -- or in some instances a *known* -- probability of being selected in a sample, then that sample will be representative of the population.

Thus, it is Gallup's goal in selecting samples to allow every adult American an equal or known chance of falling into the sample. How that is done, of course, is the key to the success or failure of the process.

Selecting a Random Sample

To conduct a national opinion poll, Gallup first chooses a method by which all or most Americans have an equal or known likely chance to be selected. Of course, most Americans have a place of residence, making it immediately obvious that if it were possible to sample for a list of all residential addresses in the country, the principle of comprehensive sampling frame could be achieved.

With this in mind, Gallup interviewers conducted the earliest polls in person by selecting places of residences from all possible geographic areas within the country and then fanning out across the country knocking on Americans' doors. This was the standard method of interviewing for nearly 50 years, from about 1935 to the mid-1980s, and it was a demonstrably reliable method.

Gallup polls across the 12 presidential elections held between 1936 and 1984 were highly accurate, with the average error in Gallup's final estimate of the election being less than three percentage points.

It became obvious over time that household sampling with in-home interviewing had problems. For one thing, it was increasingly expensive. Americans became increasingly resistant to allowing interviewers to come into their homes to conduct surveys. And the need for rapidly gathered data made the in-home interview procedure less and less attractive.

Gallup then turned its attention to the telephone. By 1986, a sufficient proportion of American households had at least one telephone to make telephone interviewing a viable and substantially less expensive alternative to the in-person method. By the end of the 1980s, Gallup was conducting the vast majority of its national surveys by telephone.

Another important change was becoming obvious by the mid- to late 2000s: the increasing use of cell phones by Americans. As a result, by 2008, Gallup had shifted its interviewing to include traditional landline and cell phone sampling. Today, with increasing shifts in communication that may eventually move some Americans beyond any type of phone toward texting and written communication, there has been increased attention on the part of survey professionals to the possible benefits of a move back to "old-fashioned" residential, address-based sampling.

For now, however, the vast majority of Gallup surveys intended to represent the national population are based on interviews conducted by landline and cell telephones. This method builds off of the central assumption that most Americans still either live in a residence with a telephone or own a personal cell phone. So, reaching people on their telephones is the starting place for current national surveys.

Procedurally, Gallup includes several steps in putting together its poll with the objective of letting every American household and every American adult have an equal chance of falling into the sample.

Initially, Gallup clearly identifies and describes the population that a given poll is attempting to represent.

If Gallup was polling about baseball fans on behalf of the sports page of a major newspaper, the target population might be all Americans aged 18 and older who say they are fans of the sport of baseball. If the poll were being conducted on behalf of Major League Baseball, however, the target audience the client requires might more specific, such as people aged 12 and older who watch at least five hours of MLB games on television, or in-person, each week. And so on.

In the case of Gallup polls that track elections and major political, social, and economic questions of the day, the target audience is generally referred to as "national adults." Strictly speaking, the target audience is all adults, aged 18 and older, living in United States. In effect, the population represented becomes all Americans aged 18 and older who have a telephone.

Next, Gallup chooses or designs a method to sample the target population randomly.

The findings from Gallup's telephone surveys are based on Gallup's standard national telephone samples, consisting of directory-assisted random-digit telephone samples using a proportionate, stratified sampling design. This complicated process starts with a computerized list of all

telephone exchanges in America, residential and cellular, along with estimates of the number of phones these exchanges have attached to them. The computer, using a procedure called random-digit-dialing (RDD), actually creates phone numbers from those exchanges and then generates telephone samples from those. In essence, this procedure creates a list of all possible household phone numbers and all possible cell phone numbers in America and then selects a subset of numbers from that list for Gallup interviewers to call.

It's important to go through this complicated procedure for two reasons. A significant percentage of residential phones are unlisted. And, almost all cell phone numbers are unlisted in the sense that there is no phone book or other comprehensive listing of them. The random-digit-dial procedure allows telephone exchanges to be the main medium of sampling, with the digits of particular phone numbers added randomly.

Selecting the Individual to Be Interviewed

Within each contacted household reached via landline, an interview is sought with the adult 18 years of age or older living in the household who has had the most recent birthday. (This is a method pollsters commonly use to make a random selection within households without having to ask the respondent to provide a complete roster of all adults living in the household). Gallup does not use the same respondent selection procedure when making calls to cell phones because they are typically associated with one individual rather than shared among several members of a household.

The Number of Interviews or Sample Size Required

One key question faced by Gallup statisticians is how many interviews does it take to provide an adequate cross section of Americans? The answer is not many -- if the respondents to be interviewed are selected entirely at random, giving every adult American an equal or known probability of falling into the sample. The typical sample size for a Gallup poll, either a traditional stand-alone poll or one night's interviewing from Gallup's Daily tracking, is 1,000 national adults.

Broadly speaking, the actual number of people that need to be interviewed for a given sample is to some degree less important than the soundness of the fundamental equal probability of selection principle. This is something many people find hard to believe, if respondents are *not* selected randomly, Gallup could have a poll with a million people and still be significantly less likely to represent the views of all Americans than a much smaller sample of 1,000 people selected randomly.

To be sure, there is some gain in sampling accuracy that comes from increasing sample sizes. Using common sense and sampling theory, a sample of 1,000 people is most likely going to be more accurate than a sample of 20. Surprisingly, however, once the survey sample approaches 500, 600, 700, or more, there are fewer and fewer accuracy gains that come from increasing the sample size. Gallup and other major organizations use sample sizes of between 1,000 and 1,500 for standard surveys because they provide a solid balance of accuracy against the increased economic cost of larger and larger samples. If Gallup were to use a sample of 4,000 randomly selected adults each time it did a poll, the increase in accuracy over a well-done sample of 1,000 would be minimal, and for sample accuracy reasons, would not justify the increase in cost.

There are, however, other reasons why large sample sizes can be important including, in particular, the ability to subset the sample into small population segments for analysis purposes. This is the great advantage provided by aggregates of Gallup's Daily tracking samples.

Statisticians over the years have developed specific ways of measuring the accuracy of samples -- so long as the fundamental principle of equal or known probability of selection is adhered to when the sample is drawn.

For example, with a sample size of 1,000 national adults (derived using careful random selection procedures), the results are highly likely to be accurate within a margin of error of ± 4 percentage points. Thus, if a president's approval rating is 50%, the margin of error indicates that the true rating (that is, the rating that would be obtained had Gallup interviewed every adult in American) is likely to be between 54% and 46%. It is unlikely to be higher or lower than that.

To be more specific, the laws of probability say that if Gallup was to conduct the same survey 100 times, asking people in each survey to rate the job President X is doing as president, in 95 out of those 100 polls, his rating would be between 46% and 54%. In five of those surveys, his rating would be higher or lower than that due to chance error.

If Gallup increases a poll sample size to 2,000, the results would then be accurate within $\pm 2\%$ of the underlying population value, a gain of two percentage points in terms of accuracy, but with a 100% increase in the cost of conducting the survey. These are the cost value decisions that Gallup and other survey organizations make when they decide on sample sizes for their surveys.

Weighting the Sample

After Gallup collects and processes survey data, each respondent is assigned a weight so that the demographic characteristics of the total weighted sample of respondents match the latest estimates of the demographic characteristics of the adult population available from the U.S. Census Bureau. Gallup weights data to census estimates for gender, race, age, educational attainment, and region.

Sec 5.2

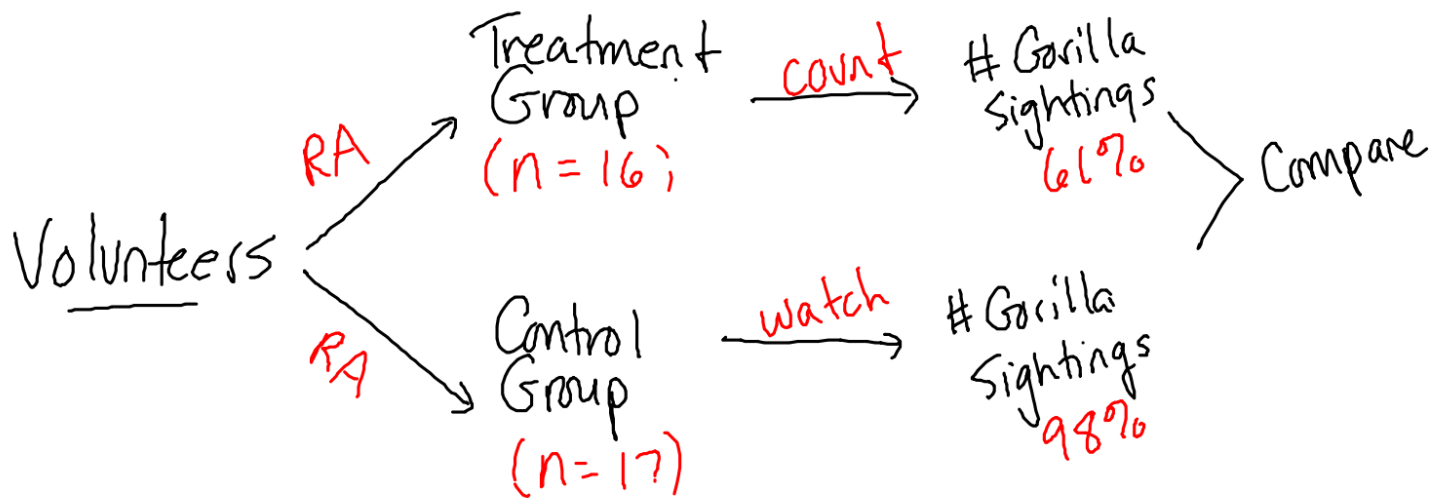
Experimental Studies

- Deliberately impose a "treatment" to influence a response
- Common on AP Exams

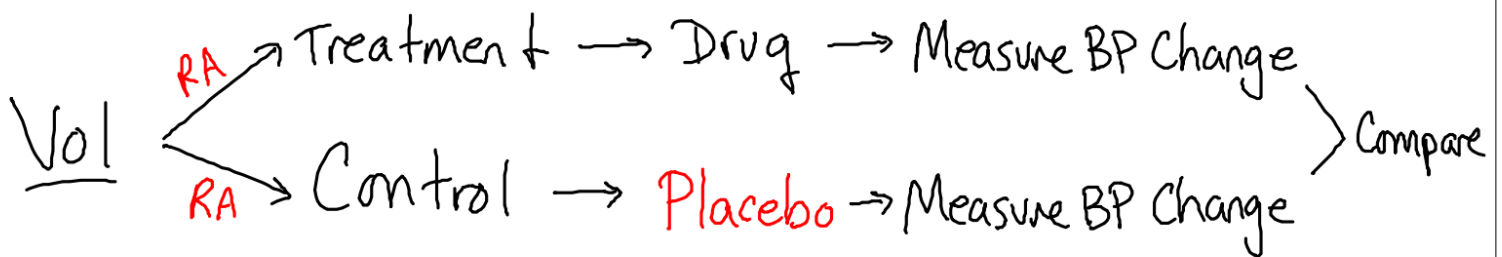
Types of Designs

- 1) Independent Samples / Between Groups
 - Blocking
- 2) Repeated Measures / Within Groups
 - Matched Pairs

Between Groups (Harvard Study)



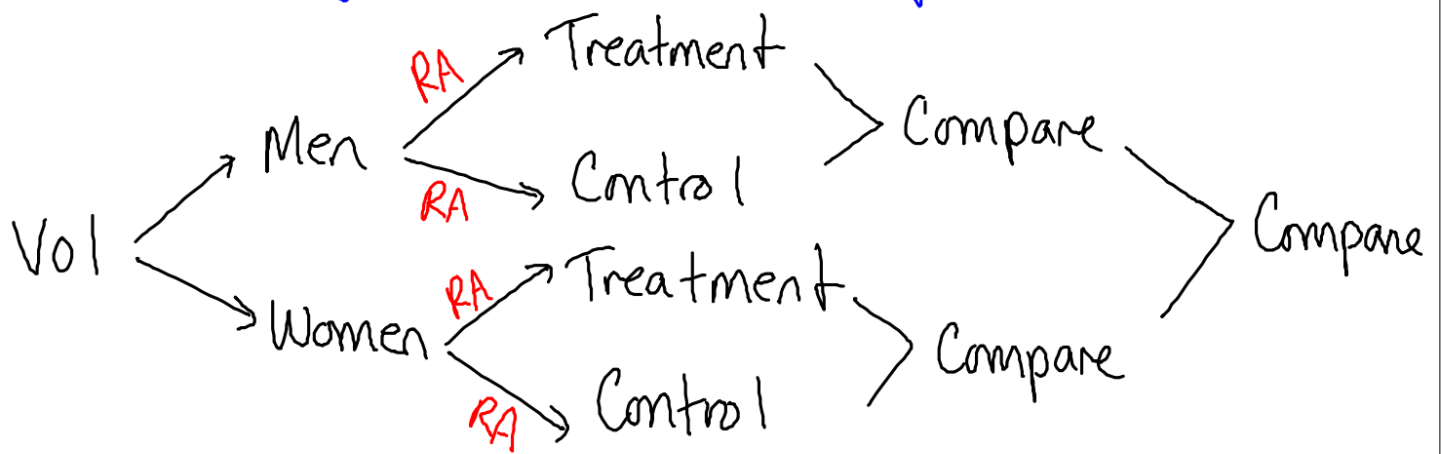
Between Groups (Blood Pressure Drug)



Placebo Effect

- 1) Large # volunteers
- 2) Double Blind Study - neither subject nor "experimenter" knows which is which

Block Designs (Based on Lurking Variable(s))

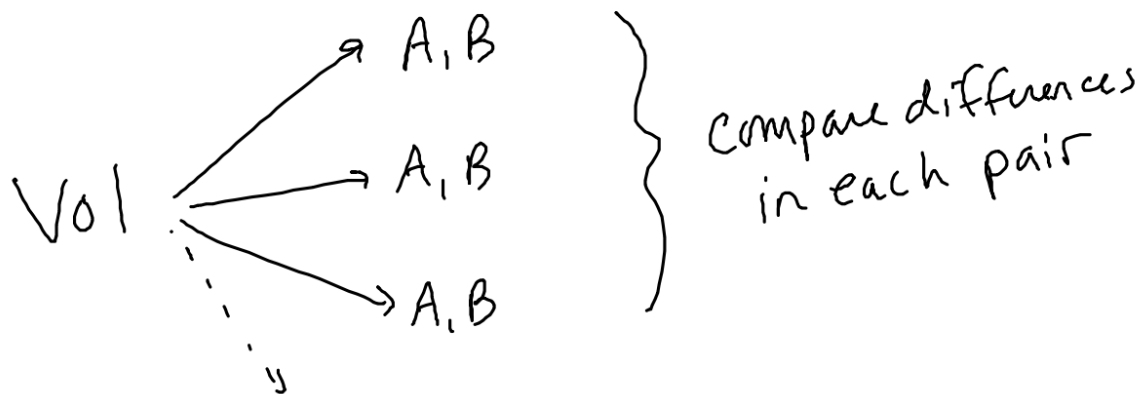


Within Groups (SAT... Prep Me)

	1	2	3	4	5	...	n
Take SAT	1100	1200	900	800	1000		X
SAT PrepMe Course							
Take SAT	1200	1100	1000	850	950		Y
Score Difference	100	-100	100	50	-50		Y-X

> Compare to 0

Matched Pairs (IQ, Gender, Race...)



Summary

C - Control everything possible

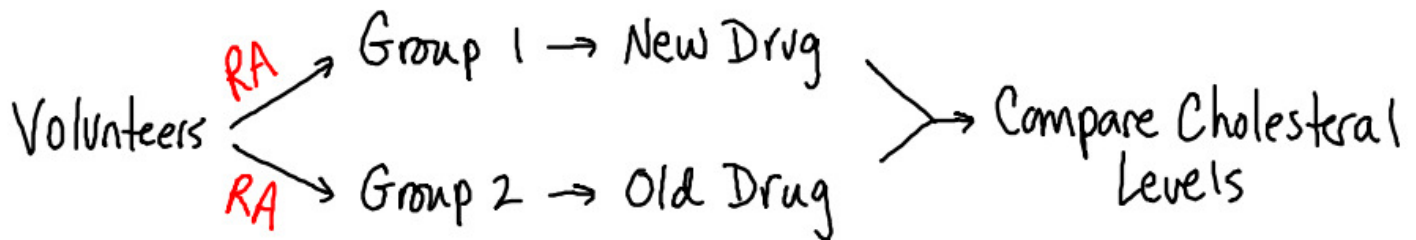
B - Block when appropriate

R - Randomize everything else

2000 AP® STATISTICS FREE-RESPONSE QUESTIONS

5. High cholesterol level in people can be reduced by exercise or by drug treatment. A pharmaceutical company has developed a new cholesterol-reducing drug. Researchers would like to compare its effects to the effects of the cholesterol-reducing drug that is currently available on the market. Volunteers who have a history of high cholesterol and who are currently not on medication will be recruited to participate in a study.

(a) Explain how you would carry out a completely randomized experiment for the study.



(b) Describe an experimental design that would improve the design in (a) by incorporating blocking.

Divide into any of the following blocks which may relate to cholesterol levels:

- Age
- Diet
- Exercise
- Gender
- Heredity

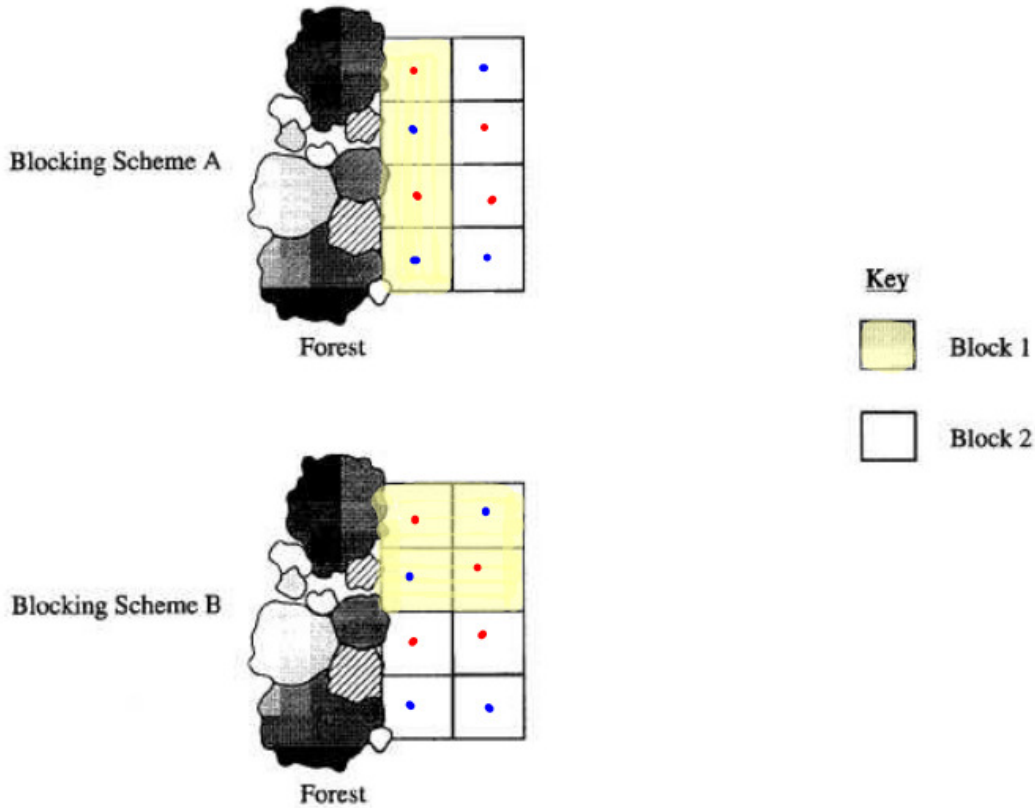
(c) Can the experimental design in (b) be carried out in a double blind manner? Explain.

Yes - as long as neither the researcher nor the subject know which drug is being used

2001 AP[®] STATISTICS FREE-RESPONSE QUESTIONS

4. Students are designing an experiment to compare the productivity of two varieties of dwarf fruit trees. The site for the experiment is a field that is bordered by a densely forested area on the west (left) side. The field has been divided into eight plots of approximately the same area. The students have decided that the test plots should be blocked. Four trees, two of each of the two varieties, will be assigned at random to the four plots within each block, with one tree planted in each plot.

The two blocking schemes shown below are under consideration. For each scheme, one block is indicated by the white region and the other block is indicated by the gray region in the figures.



- (a) Which of the blocking schemes, A or B, is better for this experiment? Explain your answer.
- (b) Even though the students have decided to block, they must randomly assign the varieties of trees to the plots within each block. What is the purpose of this randomization in the context of this experiment?

Sec 5.3

Simulation

The imitation of chance behavior
in real life

A couple wants to have children until they have a girl or until they have 4 children

1) Assume/state probability

$$P(\text{boy}) = .5 \quad P(\text{girl}) = .5$$

2) Determine a scheme

Flip Coin \rightarrow Head (Boy), Tail (Girl)

Roll Die \rightarrow Even (Boy), Odd (Girl)

Use Digits $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\} \rightarrow$
0-4 (Boy)
5-9 (Girl)

3) Perform simulation many times

1B	2B	5G	0B	4B	1B	0B	7G	5G	5G
9G	2B		3B	7G	5G	7G			
	3B		4B						
	9G		0B						

5G	2B	1B	8G	6G	9G	9G	3B	4B	0B
	7G	1B					0B	6G	2B
		3B					7G		2B
		8G							7G

4) State Conclusion

$$P(\text{Girl}) = 19/20 = 95\%$$

$$P(\text{Exactly 2 Children}) = 6/20 = 30\%$$

Misc Schemes

$P(A)$

$P(B)$

Scheme

75%

25%

$A = 001-075$ $B = 076-100$

(3 : 1)

$A = 1-3$ $B = 4$

40%

60%

$A = 001-040$ $B = 041-100$

$A = 0-3$ $B = 4-9$

$A = 6-9$ $B = 0-5$

APPS → Prob Sim ?

2001 AP® STATISTICS FREE-RESPONSE QUESTIONS

3. Every Monday a local radio station gives coupons away to 50 people who correctly answer a question about a news fact from the previous day's newspaper. The coupons given away are numbered from 1 to 50, with the first person receiving coupon 1, the second person receiving coupon 2, and so on, until all 50 coupons are given away. On the following Saturday, the radio station randomly draws numbers from 1 to 50 and awards cash prizes to the holders of the coupons with these numbers. Numbers continue to be drawn without replacement until the total amount awarded first equals or exceeds \$300. If selected, coupons 1 through 5 each have a cash value of \$200, coupons 6 through 20 each have a cash value of \$100, and coupons 21 through 50 each have a cash value of \$50.
- (a) Explain how you would conduct a simulation using the random number table provided below to estimate the distribution of the number of prize winners each week.
- (b) Perform your simulation 3 times. (That is, run 3 trials of your simulation.) Start at the leftmost digit in the first row of the table and move across. Make your procedure clear so that someone can follow what you did. You must do this by marking directly on or above the table. Report the number of winners in each of your 3 trials.

72749 13347 65030 26128 49067 02904 49953 74674 94617 13317

81638 36566 42709 33717 59943 12027 46547 61303 46699 76423

38449 46438 91579 01907 72146 05764 22400 94490 49833 09258

Sources of Data

Observational Studies

Surveys/Polls

Experiments

Control

Randomization

Replication

Principles

Between Groups (Blocking)

Within Groups (Matched Pairs)

Designs

Voluntary

Convenience

Undercoverage

Nonresponse

Response Bias

Wording

Sample Size

Random Digit

Calculator

Variations

Stratified

Multi-Stage

Systematic

SRS

Probability

Scheme

Repetitions

Conclusion

Simulations